

Special Case Equations

Name _____ Date _____

Each of these scales is balanced. Choose a number to fill into the boxes in each problem that will keep the scale balanced. You may only choose one number per problem and must plug the same number into all of the boxes

1. Any # will work to make this true.

15		15
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▲

Infinite solutions

2. The only # that works is 8

8	8		16
8	8		16

▲

ONE SOLUTION

3. NOT POSSIBLE

20		13

▲

NO SOLUTION

4. Any # will work.

7		7
7		7

▲

Infinite

5. The # that works is 10

	10		
10	10		30

▲

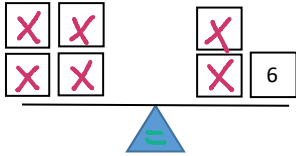
6. Not Possible

20		

▲

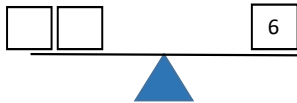
One Solution

- Only one number works



Equation

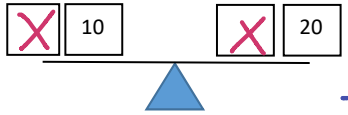
$$\begin{array}{r} 4x = 2x + 6 \\ -2x \quad | \quad -2x \\ \hline 2x = 6 \\ \frac{2x}{2} = \frac{6}{2} \\ \boxed{x=3} \end{array}$$



$x=3$ only possible answer.

No Solution

- No possible number that can work



Equation

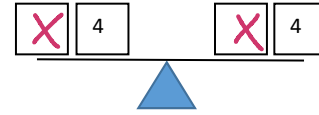
$$\begin{array}{r} x + 10 = x + 20 \\ -x \quad | \quad -x \\ \hline 10 \neq 20 \\ \text{NO SOLUTION} \end{array}$$



* all variables were eliminated & equation isn't balanced.

Infinite Solutions

- All numbers can work



Equation

$$\begin{array}{r} x + 4 = x + 4 \\ -x \quad | \quad -x \\ \hline 4 = 4 \leftarrow \\ \text{Infinite Sol.} \end{array}$$



$$\begin{array}{r|l} x+3 & = 5 \\ -3 & -3 \\ \hline \end{array}$$

$x=2$

$$\begin{array}{r|l} \cancel{5x}+5 & = \cancel{5x}+3 \\ -\cancel{5x} & -\cancel{5x} \\ \hline \end{array}$$

$5=3$
NO SOL

$$\begin{array}{r|l} 7x+3 & = 7x+3 \\ -7x & -7x \\ \hline \end{array}$$

$3=3$ Inf.

$$\begin{array}{r|l} \underline{4x}+2 & = \underline{2x}+4 \\ -2x & +2x \\ \hline \end{array}$$

$2x+2=4$

$$x + x + 3 = 2(x + 3)$$

$$\underline{2x} + \textcircled{3} = \underline{2x} + \textcircled{6}$$

NO SOL.