

NAME: _____ PERIOD: _____ DATE: _____

Homework Problem Set

+ Answers in parts A/B are found by adding & subtracting 2 original equations w/o solving for x and y first

1. Try to answer the following without solving for x and y first.

If $3x + 2y = 6$ and $x + y = 4$, then

A. $2x + y = ?$

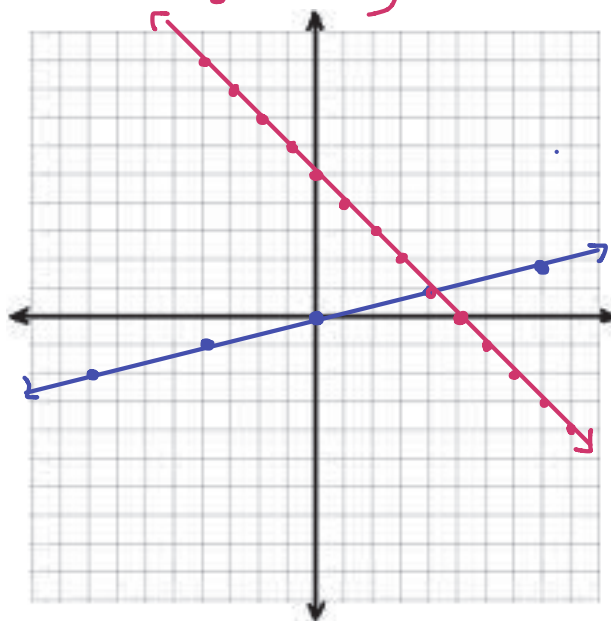
$2x + y = 2$
(subtract equations)

B. $4x + 3y = ?$

$4x + 3y = 10$
(add equations)

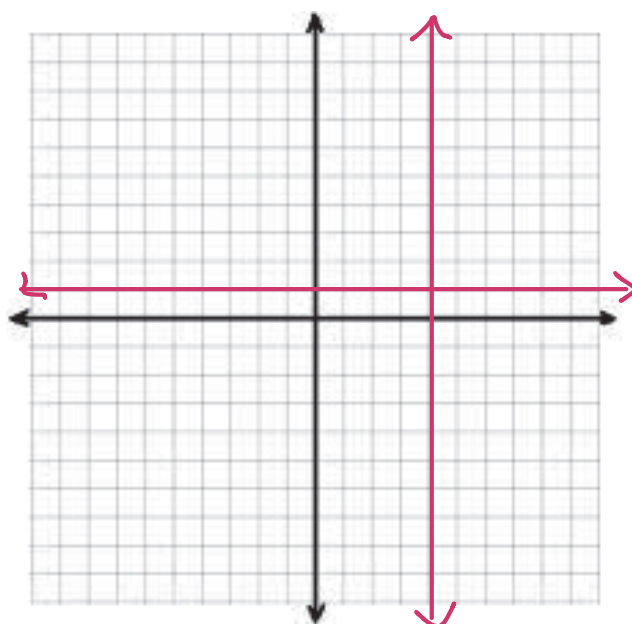
2. Solve the system of equations $\begin{cases} y = \frac{1}{4}x \\ y = -x + 5 \end{cases}$ by graphing.

$(4, 1)$



3. Create a new system of equations that has the same solution as Problem 2. Show either algebraically or graphically that the systems have the same solution.

possible answer
 $x = 4$
 $y = 1$



4. Without solving the systems, explain why the following systems must have the same solution.

System (i): $4x - 5y = 13$
 $3x + 6y = 11$

System (ii): $8x - 10y = 26$
 $x - 11y = 2$

- * 1st equation in system(ii) was obtained by multiplying the 1st equation in system(i) by 2
- * 2nd equation in system(ii) was obtained by subtracting both equations in system(i)

$$2(4x - 5y = 13) = 8x - 10y = 26$$

$$\begin{array}{r} 4x - 5y = 13 \\ - (3x + 6y = 11) \\ \hline x - 11y = 2 \end{array}$$

Solve each system of equations by writing a new system that eliminates one of the variables.

5. $2x + y = 25 \longrightarrow -2(2x + y = 25) \longrightarrow$
 $4x + 3y = 9 \longrightarrow 4x + 3y = 9 \longrightarrow$

$$\begin{array}{r} -4x - 2y = -50 \\ + 4x + 3y = 9 \\ \hline y = -41 \end{array}$$

$$\begin{array}{r} 2x + y = 25 \\ 2x - 41 = 25 \\ \hline 2x = 66 \\ x = \frac{66}{2} \\ \hline x = 33 \end{array}$$

$$\begin{array}{l} x = 33 \\ y = -41 \end{array}$$

6. $3x + 2y = 4 \longrightarrow -4(3x + 2y) = 4$
 $4x + 7y = 1 \longrightarrow 3(4x + 7y) = 1$

$$\begin{array}{r} -12x - 8y = -16 \\ 12x + 21y = 3 \\ \hline 13y = -13 \\ \hline y = -1 \end{array}$$

$$\begin{array}{r} 3x + 2y = 4 \\ 3x + 2(-1) = 4 \\ \hline 3x - 2 = 4 \\ 3x = 6 \\ \hline x = 2 \end{array}$$

$$\begin{array}{l} x = 2 \\ y = -1 \end{array}$$