

NAME: _____ PERIOD: _____ DATE: _____

Homework Problem Set

Determine the value of the variable in each equation.

1. $\frac{1}{2}x = 7$

$$\cancel{2} \cdot \frac{1}{\cancel{2}}x = 7 \cdot \frac{2}{1}$$

$$x = 14$$

2. $\frac{1}{4}y - 1 = 4$

$$\frac{1}{4}y - 1 = 4$$

$$\frac{1}{4}y - 1 + 1 = 4 + 1$$

$$\frac{1}{4}y = 5$$

$$y = 20$$

3. $b + \frac{1}{3} = \frac{2}{3}$

$$b + \frac{1}{3} = \frac{2}{3}$$

$$b + \frac{1}{3} - \frac{1}{3} = \frac{2}{3} - \frac{1}{3}$$

$$b = \frac{1}{3}$$

4. $\frac{x}{3} = 8$

$$\cancel{3} \cdot \frac{x}{\cancel{3}} = 8 \cdot 3$$

$$x = 24$$

5. $\frac{w}{5} = -2$

$$\cancel{5} \cdot \frac{w}{\cancel{5}} = -2 \cdot 5$$

$$w = -10$$

6. $c - \frac{1}{4} = \frac{3}{4}$

$$c - \frac{1}{4} = \frac{3}{4}$$

$$c - \frac{1}{4} + \frac{1}{4} = \frac{3}{4} + \frac{1}{4}$$

$$c = \frac{4}{4} \rightarrow c = 1$$

7. $\frac{m}{4} = -3$

$$\cancel{4} \cdot \frac{m}{\cancel{4}} = -3 \cdot 4$$

$$m = -12$$

8. $\frac{-2r}{7} = 6$

$$\frac{-\cancel{2}r}{\cancel{7}} = 6 \cdot \frac{7}{-\cancel{2}}$$

$$r = \frac{42}{-2} \rightarrow r = -21$$

9. $-5 = \frac{-x}{6}$

$$6 \cdot -5 = \frac{-x}{\cancel{6}} \cdot \cancel{6}$$

$$\frac{-30}{-1} = \frac{-x}{-1} \rightarrow x = 30$$

10. $-\frac{5}{6}p = \frac{3}{4}$

$$\frac{\cancel{6}}{\cancel{6}} \cdot \frac{-5}{\cancel{6}}p = \frac{3}{4} \cdot \frac{\cancel{6}}{\cancel{6}}$$

$$p = \frac{18}{-20} \rightarrow p = -\frac{9}{10}$$

11. $\frac{3n}{4} = \frac{-1}{2}$

$$\frac{\cancel{4}}{\cancel{4}} \cdot \frac{3n}{\cancel{4}} = \frac{-1}{2} \cdot \frac{\cancel{4}}{\cancel{3}}$$

$$n = \frac{2}{3}$$

12. $2y - \frac{3}{5} = \frac{1}{2}$

$$2y - \frac{3}{5} = \frac{1}{2} = \frac{5}{10}$$

$$2y - \frac{3}{5} + \frac{3}{5} = \frac{5}{10} + \frac{3}{5} = \frac{6}{10}$$

$$\frac{1}{\cancel{2}} \cdot \cancel{2}y = \frac{11}{10} \cdot \frac{1}{\cancel{2}}$$

$$y = \frac{11}{20}$$

13. $\frac{1}{4}x + x = -3 + \frac{1}{2}x$

LCD: 4
 $4\left(\frac{1}{4}x + x\right) = (-3 + \frac{1}{2}x)4$
 $x + 4x = -12 + 2x$
 $5x - 2x = -12 + 2x - 2x$
 $3x = -12$
 $\frac{3x}{3} = \frac{-12}{3}$ $x = -4$

14. $\frac{1}{3} + 2m = m - \frac{3}{2}$

LCD: 6
 $6\left(\frac{1}{3} + 2m\right) = (m - \frac{3}{2})6$
 $2 + 12m = 6m - 9$
 $-6m - 6m$
 $2 + 6m = -9$
 $-2 -2$
 $6m = -11$
 $\frac{6m}{6} = \frac{-11}{6}$ $m = -\frac{11}{6}$

15. $b + \frac{2}{3} = \frac{1}{4}b - 1$

LCD: 12
 $12\left(b + \frac{2}{3}\right) = (\frac{1}{4}b - 1)12$
 $12b + 8 = 3b - 12$
 $-3b -3b$
 $9b + 8 = -12$
 $9b = -20$ $b = -\frac{20}{9}$

16. $\frac{2}{5}(w - 2) = -3$

$\frac{5}{2} \cdot \frac{2}{5}(w - 2) = -3 \cdot \frac{5}{2}$
 $w - 2 = -\frac{15}{2}$
 $w - \frac{4}{2} = -\frac{15}{2}$
 $+\frac{4}{2} +\frac{4}{2}$
 $w = -\frac{11}{2}$

17. $\frac{3}{4}(2m + 1) = 2$

$\frac{4}{3} \cdot \frac{3}{4}(2m + 1) = 2 \cdot \frac{4}{3}$
 $2m + 1 = \frac{8}{3}$
 $2m + \frac{3}{3} = \frac{8}{3}$
 $\frac{1}{2} \cdot 2m = \frac{5}{3} \cdot \frac{1}{2}$
 $m = \frac{5}{6}$

18. $\frac{2}{3}(3p + 1) = 5$

$\frac{3}{2} \cdot \frac{2}{3}(3p + 1) = 5 \cdot \frac{3}{2}$
 $3p + 1 = \frac{15}{2}$
 $3p + \frac{2}{2} = \frac{15}{2}$
 $\frac{1}{3} \cdot 3p = \frac{13}{2} \cdot \frac{1}{3}$
 $p = \frac{13}{6}$

19. $\frac{x}{10} + \frac{3x}{5} = \frac{7}{2}$

LCD: 10
 $10\left(\frac{x}{10} + \frac{3x}{5}\right) = \left(\frac{7}{2}\right)10$
 $x + 6x = 35$
 $7x = 35$
 $\frac{7x}{7} = \frac{35}{7}$
 $x = 5$

LCD: 6
 $12 - \frac{4m}{3} = \frac{m}{6}$

$6\left(12 - \frac{4m}{3}\right) = \left(\frac{m}{6}\right)6$
 $72 - 8m = m$
 $72 = 9m$
 $\frac{72}{9} = \frac{9m}{9}$ $m = 8$

21. $\frac{4y}{9} - \frac{2y}{3} = 10$

LCD: 9
 $9\left(\frac{4y}{9} - \frac{2y}{3}\right) = (10)9$
 $4y - 6y = 90$
 $-2y = 90$
 $\frac{-2y}{-2} = \frac{90}{-2}$
 $y = -45$

22. $\frac{y+3}{5} - \frac{3y}{10} = 7$

LCD: 10
 $10\left(\frac{y+3}{5} - \frac{3y}{10}\right) = (7)10$
 $2(y+3) - 3y = 70$
 $2y + 6 - 3y = 70$
 $-y + 6 = 70$
 $-\frac{y}{-1} = \frac{64}{-1}$ $y = -64$

23. $\frac{x-4}{4} - \frac{x}{3} = 6$

LCD: 12
 $12\left(\frac{x-4}{4} - \frac{x}{3}\right) = (6)12$
 $3(x-4) - 4x = 72$
 $3x - 12 - 4x = 72$
 $-x - 12 = 72$
 $-x = 84$
 $x = -84$

24. $\frac{b+5}{3} + 4 = -16$

LCD: 3
 $3\left(\frac{b+5}{3} + 4\right) = (-16)3$
 $b + 5 + 12 = -48$
 $b + 17 = -48$
 $b = -65$

REVIEW—Lowest Common Denominator (LCD)

Determine the LCD of each set of functions.

25. $\frac{1}{3}, \frac{1}{6}, \frac{1}{9}$

LCD = 18

3: 3, 6, 9, 12, 15, 18, 21
 6: 6, 12, 18, 24
 9: 9, 18, 27

26. $\frac{1}{2}, \frac{1}{4}, \frac{3}{8}$

LCD = 8

2: 2, 4, 6, 8, 10, 12, 14, 16, 18
 4: 4, 8, 12, 16, 20, 24
 8: 8, 16, 24, 32

27. $\frac{2}{5}, \frac{1}{3}$

LCD = 15

28. $\frac{2}{5}, \frac{1}{3}, \frac{2}{3}$

LCD = 15

29. $\frac{2}{5}, \frac{1}{3}, \frac{5}{2}$

LCD = 30

30. $\frac{7}{8}, \frac{3}{16}, \frac{4}{32}$

LCD = 32

31. $\frac{1}{2}, \frac{1}{3}, \frac{1}{4}$

LCD = 12

32. $5, \frac{6}{7}$

LCD = 7

33. $\frac{10}{11}, \frac{19}{22}, \frac{1}{2}$

LCD = 22

34. $\frac{5}{6}, \frac{7}{8}, \frac{9}{10}$

LCD = 120

Spiral REVIEW—Solving Equations

Determine the value of the variable in each equation. Check your solutions.

35. $2(2 - 3x) = 3(3 + x) + 4$

$$4 - 6x = 9 + 3x + 4$$

$$4 - 6x = 13 + 3x$$

$$4 = 13 + 9x$$

$$-9 = 9x$$

$$x = -1$$

37. $14 - (6 - 3c) = 4c - c$

$$14 - 6 + 3c = 4c - c$$

$$8 + 3c = 3c$$

$$-3c \quad -3c$$

$$8 = 0$$

$$\text{No Solution}$$

39. $3(3h - 1) = 4(h + 3)$

$$9h - 3 = 4h + 12$$

$$5h = 15$$

$$h = 3$$

41. $1 - 2t = 2(1 - t)$

$$1 - 2t = 2 - 2t$$

$$+2t \quad +2t$$

$$1 \neq 2$$

$$\text{No Solution}$$

43. $-9x + 12x = 3(2 - x)$

$$3x = 6 - 3x$$

$$+3x \quad +3x$$

$$6x = 6$$

$$x = 1$$

36. $5(m + 1) + 6 = 3(4 + m) + (2m - 1)$

$$5m + 5 + 6 = 12 + 3m + 2m - 1$$

$$5m + 11 = 5m + 11$$

$$-5m \quad -5m$$

$$11 = 11$$

$$\text{Infinite Solutions}$$

38. $3y - 2(y - 19) = 9y - 3(9 - y)$

$$3y - 2y + 38 = 9y - 27 + 3y$$

$$y + 38 = 12y - 27$$

$$38 = 11y - 27$$

$$65 = 11y$$

$$y = \frac{65}{11}$$

40. $(5t + 9) - (3t - 13) = 2(11 + 2t)$

$$5t + 9 - 3t + 13 = 22 + 4t$$

$$2t + 22 = 4t + 22$$

$$22 = 2t + 22$$

$$0 = 2t$$

$$t = 0$$

42. $5(3 - m) = 15m + 15$

$$15 - 5m = 15m + 15$$

$$15 = 10m + 15$$

$$0 = 10m$$

$$m = 0$$

44. $10(0.2 + 0.4c) = 10c + 0.2 - 6c$

$$2 + 4c = 4c + 0.2$$

$$-4c \quad -4c$$

$$2 \neq 0.2$$

$$\text{No solution}$$